MAKER: Very Low Cost Experiments via 3-D Printing and Vacuum Forming

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Abstract

We demonstrate a new approach to fabricate inexpensive fluid and thermal experiments that engineering students can manipulate to master concepts in thermodynamics, fluid mechanics and heat transfer. The approach is based on design for manufacture that leverages flexible manufacturing tools such as CAD, 3-D printers and vacuum forming machines to produce an array of simple and easy to use experimental hardware. Several sets of experimental hardware have been developed: Venturi Nozzle experiments conceived to exercise students’ understanding of the Bernoulli equation and Pipe Flow experiments designed to help students’ master principles of head loss. The experimental devices to be demonstrated here have been fabricated using a four step approach. First, commercial CAD software is used to define the geometry of an experiment. Second, a rapid prototyping machine is used to 3-D print a plastic mold of the design. Third, a vacuum former is used to form thin plastic sheets around the 3-printed mold. Finally, the vacuum formed sheets are assembled together to produce multiple copies of the experiment. The result is an approach that allows the development of experiments that are robust and inexpensive enough to distribute individual copies to small groups of students with the cost to each student in the class comparable to the price of a textbook. This approach opens up the possibility of a wide variety of experimental activities for active learning that can be implemented in classrooms, for home use, and for distance education.

Introduction

Unfortunately, much student learning in classrooms revolves around passively listening to traditional lectures followed by solving textbook problems. While lectures may transmit facts and solving textbook problems encourages the development of procedural knowledge, neither approach is effective in developing a deeper conceptual understanding of engineering topics. The present work aims to overcome these deficiencies in common classroom techniques by providing students with simple, inexpensive experimental devices, which students can manipulate in the classroom, to stimulate active learning of important engineering concepts.

Active learning, especially experiential learning, has been shown by many educational researchers to result in superior learning outcomes than traditional delivery methods like lecturing. As a result, educators have developed various active learning activities based on experiments that students can manipulate and learn firsthand for themselves. Several approaches have been taken, with some researchers focusing on take-home experiments that students can undertake as homework, others developing experiments that can be accessed remotely for distance education, and a third group designing experiments for in-class use.
In an example of this first group, T. Scott reported on two fluid mechanics experiments designed to be completed as homework assignments by students in a fluid mechanics course. Students were asked to assemble and use two simple experimental devices. First, the students used a hydrometer to measure and report the specific gravity of common household fluids. Second the students assembled a water manometer from vinyl tubing and used it to measure the differential pressure across the side window of a moving car. In each case the cost of the experimental apparatus was minimal, while the experience of doing the experiments appeared to enhance the students’ understanding of the basic concepts involved. Cimbala et al. took a similar approach and developed a take-home experiment in which students characterized the performance of a small aquarium pump, and compared their results with the manufacturer’s pump curve. The entire experimental apparatus cost less than $20 for each student, but resulted in a significant gain in learning.

A number of education researchers have developed experiments that can be accessed remotely, so that students can manipulate engineering hardware via the internet. Ogot et al. reported on a jet thrust laboratory that students could access on-line, and perform remotely. In this case, the experimental apparatus was assembled from high quality components and housed and maintained in a traditional laboratory setting. Cost savings came not from reducing the price of hardware, but from making expensive hardware more freely available. In addition, interaction with the experiment came not from hands-on manipulation of hardware, but via the software interface, Lab-View, and video flow visualization. However, a comparison of students performing the lab hands-on and students performing it remotely indicated statistically similar learning outcomes. Ellis et al. documented a similar remotely accessed experiment that allowed students to operate and make measurements on a Venturi nozzle. In this case an existing lab was retrofitted with internet accessible controls and data acquisition to enable students at branch campuses to remotely perform the experiment. Once again, an assessment of student learning comparing students in the lab and students using remote access indicated similar outcomes.

Finally, significant effort has been devoted to developing experiments suitable for in-class use. In this approach, the goal has been to use student-centered, hands-on experiments during regular class time to replace or supplement instructor-centered pedagogies. Early work by Van Wie et al. involved having student teams put together experiments to learn fluid flow and heat transfer concepts. Visco built on this concept, with projects exemplifying engineering concepts built, and then modified and rebuilt by subsequent student teams over the course of several years. In Visco’s model an important goal the student-built experiments was compactness, so that each could fit easily on a classroom desktop. Minnerick developed simple and inexpensive heat transfer experiments that students could easily manipulate in the classroom.

Van Wie et al. have worked to develop a system of compact experiments called Desktop Learning Modules (DLM’s) that can be brought into the classroom. The DLM system is based on a series of cartridges that can plug into a base unit with liquid reservoir, pump, and data acquisition. Each cartridge holds the hardware for a particular thermofluid experiment. Cartridges available include heat exchanger, pipe flow, fluidized bed, and
venturi nozzle experiments among others. Assessment of student learning using the DLM system has shown significant gains for students using the active learning approach.\textsuperscript{9,10} As a consequence of this success, a commercial version of the Van Wie group DLM's has been introduced by educational equipment supplier Armfield Ltd.

Active learning using thermofluid experiments has repeatedly been shown to enhance student learning, whether used outside of class for take-home assignments, for students in remote locations in distance learning environments, or brought into the classroom to supplement or replace lecture-based pedagogies. In all of these applications, a major consideration is the cost of the hardware used. For example, although the DLM’s developed by the Van Wie group have demonstrated efficacy in enhancing learning outcomes for students, a major factor impeding their widespread use is their cost. Reducing that cost would make them far more attractive. In general, for active learning strategies to be most successful there must be enough experimental stations for each student to manipulate the hardware to be actively engaged. To make this a realistic option, the cost of each station must be very low. Recent work has indicated a pathway that might significantly lower the cost of these kinds of Modules. That work has shown how very low cost thermofluid experimental hardware can be fabricated by leveraging new capabilities in CAD, 3-D printing and vacuum forming.\textsuperscript{11,12}

The present work describes recent progress based on this approach, illustrating the design and fabrication of experimental hardware that is inexpensive, simple and robust enough to allow student groups as small as two or three to have their own experimental setup. By focusing on developing means to manufacture very low-cost devices, we hope to demonstrate a path to provide experimental hardware for active learning experiences that will meet a broad range of engineering curricular needs.

Approach

The approach developed here is based on design for manufacture and leveraging new manufacturing modalities such as rapid prototyping and vacuum forming in order to produce an array of simple, inexpensive, and easy to use experimental hardware. We believe that end product cost reductions can be achieved, by designing the hardware to take advantage of specific strengths of new manufacturing routes, use of inexpensive materials, and simplicity of concept.

Leveraging New Manufacturing Techniques

Recently developed manufacturing techniques are opening up new ways to fabricate devices that can help students learn engineering concepts in ways that are more motivating and that lead to deeper understanding. Leveraging these new manufacturing approaches can enable educators to design and fabricate experimental hardware for student use in ways that are dramatically less expensive and more flexible than anything
seen up to now. These new manufacturing techniques are expected to result in products so inexpensive to produce, that there will be enough experimental hardware for every student in a course to explore.

The key to this approach is to combine two complementary ideas. First, we make design for manufacture a primary consideration, from the beginning of the development cycle for each experiment. Second, we take advantage of new fabrication tools to speed up, simplify and reduce the cost of manufacture.

In design for manufacture, the conception of each piece of experimental hardware to be produced is considered from the perspective of reducing the number of parts to the absolute minimum, designing those parts for easy assembly, and fabricating the parts using simple, fast, and flexible processes requiring little or no skilled labor, while using very low-cost, readily sourced materials. Taking advantage of new fabrication tools aids greatly in realizing products conceived through this design philosophy. In particular, we rely heavily on three current manufacturing processes: Computer Aided Design (CAD), 3-D printing and vacuum forming. Figure 1 outlines this design and fabrication strategy.

This approach, starting from defining hardware geometries using CAD, then employing 3-D printing to realize those hardware geometries in plastic molds, through producing complete devices using vacuum forming, enables very fast design, and fabrication of hardware. The time to realize a proposed experimental device from conception to finished prototype can be as low as one week. As a result, we can run through multiple design, build, and test iterations on proposed experiments over the course of semester. Quick iteration of the design cycle in turn, greatly aids in the task of developing experiments that students find appealing and easy to work with.
One particularly appealing advantage of the proposed fabrication route is that it can take advantage of the tight integration between widely used CAD software and 3-D printers. That is, it enables hardware design via CAD, simplifying the specification of the precise geometries necessary for the working engineering devices desired. It also means that numerical analysis software (CFD or finite element structural software) can be integrated into the design of experiments to predict and optimize device behavior. It allows multiple designers to explore alternate design paths simultaneously, and significantly speed up the design turn-around times. The use of CAD software with 3-D printed prototypes means that design iterations are expected to take hours or days instead of weeks or months as for traditionally machined parts. Likewise, costs for prototype designs are expected to be much less than for machined parts, with single iterations of an experiment costing only a few dollars for materials and processing.

A significant advantage of producing educational hardware using 3-D printers driven by CAD software is that many undergraduate mechanical engineering students now learn to use these commercial tools in introductory engineering courses (freshman and sophomore level design classes). As a result we are able to include undergraduate students in the design and fabrication of hardware. Thus, students using the experiments are able to see and understand exactly how that hardware is designed and manufactured. In addition, it should soon be possible for us to allow students using the experiments to propose their own modifications of the hardware. Quick turn-around on fabrication via 3-D printing and vacuum forming makes the option of student or instructor driven modification of experiments an appealing possibility for future work.

Design of Experiments

In order to demonstrate the present approach of the design and fabrication of very low cost experimental devices, we present two recently developed experiments: (1) a Venturi nozzle, (2) a pipe flow/head loss experiment. A third experiment: (3) a concentric pipe heat exchanger is currently in the design phase.

The venturi nozzle experiment is designed to demonstrate the way energy is transferred between static pressure and fluid velocity (or kinetic energy), as a fluid passes through a converging nozzle (conservation of mechanical energy). The pipe flow/head loss experiment illustrates how static pressure falls as a fluid moves through a pipe (conservation of energy), while fluid velocity remains constant (conservation of mass). The concentric tube heat exchanger should enable students to explore how fluid-flow rates and flow geometry, affect heat transfer rates and temperatures changes in two fluids co-flowing or counter-flowing fluids (conservation of energy & heat transfer).

For these experiments to be effective, the experimental hardware must meet several criteria. (1) The experimental hardware must be visually appealing, simple to operate and hard to break. (2) Students should be able to easily control fluid flow rates in the experiments. (3) Measurement techniques to determine fluid flow rates, pressures, and temperatures must be precise enough to minimize experimental uncertainty, while being
simple and inexpensive to implement. Measurement techniques that are easily understandable and that appeal to fundamental physical principles are the best.

The first requirement, hardware that is visually appealing, simple to operate and hard to break, is at least partially fulfilled through the choice of thin sheets of transparent PETG for the primary fabrication material. This plastic, most commonly seen in blister packaging of retail products, is inexpensive, tough and attractive. Upon vacuum forming, PETG retains a crystal-clear, smooth finish and is quite robust. A vacuum formed PETG Venturi nozzle can be dropped to the ground from chest height with no loss of function.

The second requirement, easy control of fluid flow rates, is fulfilled through the choice of small battery powered air and water pumps to move fluids. For safety and simplicity, only air and water are used as fluids in the experiments described here. As a result, battery powered water pumps designed for small water fountains and air pumps intended to blow up inflatable mattresses and water toys are sufficient for the present set of experiments. Such air and water pumps are mass marketed and can be readily purchased for very low cost. For example, we were able to purchase miniature water pumps that can produce flows of 2 L/min with a head of 2 m (9.8 kPa) while being powered by rechargeable D-cell batteries for 12 dollars. Likewise, we found air pumps that can produce flows of 1L/min, powered by D-cells for 24 dollars. The use of these inexpensive, battery-powered pumps allows each experimental set-up to be completely portable, while being very safe and simple to operate.

Water flow loops are assembled from flexible, vinyl tubing with flow control by cheap, in-line ball valves. A plastic storage box is used both as a water reservoir and a base for the experiment (either the vacuum-formed PETG Venturi Nozzle or the Pipe Flow/Head Loss hardware). Assembling a water flow loop requires only connecting the water pump, ball valve and vacuum-formed PETG experiment together, filling the reservoir with water, and then dropping four D-cell batteries into the pump’s battery box. Water flow rate is varied by adjusting the plastic ball valve.

Experiments using air as the working fluid are even simpler, since leaks are not an issue and a closed fluid loop is not required. Vacuum-formed experiments are designed to simply press fit up against the battery powered air pump. Air flow rate through the experiments is varied by restricting air flow into the pump via a set of variously sized plastic nozzles.

The third requirement is for simple, inexpensive measurement techniques for students to determine fluid flow rates, pressures and temperatures. These measurement techniques must also be sufficiently precise and repeatable to minimize experimental uncertainty. There exists a real danger that poorly designed experiments will actually hinder student learning. Such an outcome is possible if large experimental uncertainties or common measurement blunders result in students obtaining results that actually contradict the physical principles we are hoping that they will learn. Such outcomes increase student misconceptions, and undermine confidence in the concepts we hope to reinforce with these low-cost experiments. As a result, designing measurement techniques that are
accurate, easy to use and easy to understand is of crucial importance. Measurement techniques must be robust, simple to employ, as intuitive as possible to interpret, with relatively low uncertainty. If at all possible, students should be able to easily grasp the physical concepts underlying the measurement techniques.

To measure the flow rates of liquid, e.g. water, we have chosen to use a positive displacement method: a “bucket and stopwatch” technique. Water flowing out of the outlet of each experiment is caught in a 500 mL measuring cup. The time to fill the 500 mL is measured on a stopwatch. Unfortunately, we could devise no simple positive displacement method to measure the flow rates of gases, e.g. air. As a result, we purchased inexpensive turbine anemometers, designed and marketed to measure wind speeds. We found rotary vane anemometers with a precision of 0.1 m/s for a cost of 30 dollars. However, obtaining accurate air velocity measurements with these rotary vane anemometers requires a tight fit between the anemometer turbine shroud and the experiment’s outlet, and a careful accounting of cross-sectional flow area through the anemometer.

To measure pressure in all experiments, liquid (water) manometers were molded into the flow hardware. In this way, the pressure drop along the pipe flow experiment and the pressure drop and recovery through the Venturi nozzle are easily visualized as water heights in liquid columns. Thus, fluid heights give a visual indicator proportional to pressure. This approach results in two significant pedagogical advantages. First, the height of a liquid column gives an easily interpreted visual cue as to the pressures in the fluid. Second, calculating pressure from fluid height can be done by students from first principles giving students an easily-understood, measure of pressure.

Manufacture of Experiments

Several initial prototype experiments have been manufactured in our labs and implemented in undergraduate engineering classes. Two Venturi Nozzle experiments,
one designed to use air, and one designed to use water as the working fluid can be used to illustrate the proposed approach for the fabrication of the low-cost experiments.

The experimental hardware was designed using SolidWorks™ CAD software. Figure 2 (a) and (b) illustrates the CAD model developed for the Venturi nozzle experiment. Figure 2 (a) gives the dimensions of the model, while Fig. 2 (b) shows a rendering of the CAD model. The CAD models were exported to a Stratasys Uprint SE 3-D printer, to produce three dimensional representations of the experimental hardware geometries in ABS plastic. Two sets of molds, mirror images of each other, were required for each set of experimental hardware produced. An ABS plastic printout of the Venturi nozzle with manometer pressure taps taken directly from the 3-D printer is shown in Fig. 3. These 3-D printouts were then used as molds for vacuum forming. Vacuum forming was accomplished with an EZFORM LV 1827 using 0.20” thick sheets of transparent PETG. Figure 4 illustrates the PETG sheet as it appeared upon being removed from the vacuum forming machine. Each experimental device was then assembled by gluing together the two mirror-image halves vacuum-formed in PETG. This was done by first cutting excess plastic away from the PETG sheets, and then using Weld On 3 Acrylic cement to glue the two mirror image sheets together. The assembled Venturi nozzle is shown in Fig. 5. Note that the Venturi nozzle includes three manometers integrated into the nozzle entry, throat and exit for pressure measurements.

All that is required to complete the experimental hardware for the Venturi nozzle shown in Fig. 5 is to add a water flow loop. Figure 6 illustrates how this is done. In Fig. 6 a miniature water pump, along with two plastic ball valves used to control water flow rates, are connected to the PETG Venturi nozzle with flexible vinyl tubing. The water pump is powered by D-cells inserted into the battery clip connected to the pump. To run the experiment, the plastic Venturi nozzle is attached to a plastic tub with bolts, the tub is filled with water, and the water pump dropped into the water. Figure 7 shows the fully assembled experiment running.
A similar Venturi nozzle experiment using air as the working fluid was manufactured in much the same way. Figure 8 shows this Venturi nozzle in operation. In this case an air pump is used to blow air through the nozzle. Students measure the differential pressure across the nozzle with a water manometer and the velocity of the air through the Venturi with a rotary vane anemometer.

A quick cost accounting of the manufactured hardware is shown in Table 1. The material cost for one PETG Venturi nozzle was approximately $6 (including the cost of the 3-D Printed Mold):

Table 1 Cost Breakdown of the Water and Air Venturi Nozzles

<table>
<thead>
<tr>
<th></th>
<th>Water Venturi Nozzle</th>
<th>Air Venturi Nozzle</th>
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</thead>
<tbody>
<tr>
<td>3-D Printed Mold (ABS)</td>
<td>$25</td>
<td>$25</td>
</tr>
<tr>
<td>Plastic Sheet (PETG)</td>
<td>$5</td>
<td>$5</td>
</tr>
<tr>
<td>Flow Circuit Hardware</td>
<td>$12</td>
<td>$24</td>
</tr>
<tr>
<td>Pump (Air or Water)</td>
<td>$5</td>
<td>$5</td>
</tr>
<tr>
<td>Valves</td>
<td>$20</td>
<td>$25</td>
</tr>
<tr>
<td>Batteries (Rechargeable D Cells)</td>
<td>6 X $10 = $60</td>
<td>4 X $10 = $40</td>
</tr>
<tr>
<td>Plastic Carrying Box</td>
<td>$5</td>
<td>$5</td>
</tr>
<tr>
<td>Anemometer</td>
<td>-</td>
<td>$28</td>
</tr>
<tr>
<td>Measuring Cups (Metric)</td>
<td>$4</td>
<td>-</td>
</tr>
<tr>
<td>Cost per Experiment (Assuming 25 Set ups)</td>
<td>$37</td>
<td>$69</td>
</tr>
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</table>
printed mold and assuming 25 nozzles fabricated with one mold). The water pump cost $12. The battery box was $5. Each ball valve cost $2. The vinyl tubing was under $1. The plastic box used to hold all parts was $5. Excluding the cost of the 3-D printer, vacuum former and labor, then the entire water Venturi nozzle experiment cost $37 to assemble. The cost of the Pipe/Flow Head Loss experiment was similar. The air Venturi nozzle experiment was more expensive. The PETG Venturi nozzle material cost was about $5. The air pump was more expensive at $24.00. The most expensive component, the rotary vane anemometers cost $28 each. As a result the air Venturi nozzle experiment cost $69 to assemble (again excluding 3-D printer, vacuum former and labor).

Results

The Venturi nozzle experiment and a Pipe Flow/Head Loss experiment were implemented as in-classroom active learning experiences in two junior-level engineering classes: a mechanical engineering fluid mechanics course, and a chemical engineering fluid mechanics and heat transfer course. The ME fluids class served 75 students, while the ChE fluids and heat transfer class served 50 students. In both classes sufficient numbers of experimental set-ups were manufactured to allow groups of three students to have their own experiment. To this end, twenty air Venturi, twenty-five water Venturi, and twenty-five Pipe Flow/Head Loss experiments were manufactured. In order to minimize costs, the same flow loops (including water pumps with battery packs, ball valves and vinyl tubing) were used for the water Venturi and Pipe Flow/Head Loss experiments. The air Venturi utilized a separate set of air pumps.

An initial assessment of the experimental uncertainty expected for both the Venturi nozzle and Pipe Flow/Head Loss experiments was conducted. Among expected errors were errors attributable to dimensional variation caused by manufacturing tolerances, and errors attributable to fluid flow perturbations caused by flow loop entrance effects and pipe bends. The effect of dimensional variation due to manufacturing tolerances would show up as random error when testing multiple devices, but bias error when testing a
Figure 9 shows experimental results for both Venturi and Pipe Flow/Head Loss experimental hardware. Figure 9 (a) shows the results of tests run on seven PETG Venturi nozzles. On the figure, symbols indicate the pressure drop (cm H₂O) measured between the entrance and throat is plotted against the flow rate (mL/s) for each nozzle. The pressure drop predicted by Bernoulli’s equation is shown by a solid line. The random errors in the measurements are seen to fall within a band of 20%.

Figure 9 (b) shows the results of tests run on a PETG Pipe Flow/Head Loss experiments. On this figure symbols indicate the pressure drop (cm H₂O) measured along twenty centimeters of plastic pipe versus the flow rate (mL/s) through the pipe. The pressure drop predicted by the Moody Diagram is shown by a solid line. In this case, the shift from laminar to turbulent flow is clearly visible around a flow rate of 10 mL/s which corresponds to a Reynolds number of Re_D ~ 3000. The laminar to turbulent transition is apparent both in the measured (symbols) and the predicted (solid line) pressure drop measurements. However, a bias error of about + 5 mm H₂O can be seen in the pressure drops measured for the laminar regime. The measured and predicted pressure drops are in excellent agreement for the turbulent regime data. The most likely explanation for this bias error is a perturbation of the flow profile caused by the 180° bend some 4 cm upstream of the first pressure measurement. The presence of the error in the laminar data but not in the turbulent data is attributed to the much faster recovery of the turbulent flow profile than the laminar flow profile. An effort to diagnose and correct this problem in the Pipe Flow/Head Loss hardware is underway.

Conclusions

A new approach to fabricate inexpensive fluid and thermal experiments has been demonstrated. The approach is based on a design for manufacture philosophy that leverages flexible manufacturing tools to produce simple experimental hardware. The
Experimental devices were fabricated using a four step approach. First, commercial CAD software was used to define the geometry of an experiment. Second, a rapid prototyping machine was used to 3-D print a plastic mold of the design. Third, a vacuum former was used to form thin plastic sheets around the 3-printed mold. Finally, the vacuum formed sheets were assembled together to produce multiple copies of the experiment.

Two Venturi Nozzle experiments and a Pipe Flow/Head Loss experiment were developed. Sufficient copies of the hardware were manufactured to implement these experiments in junior-level mechanical engineering and chemical engineering classrooms. The cost per experimental set-up ranged from $29 dollars for the Venturi nozzle and Pipe Flow experiments using water as the working fluid, to $53 dollars for the Venturi nozzle experiment using air as the working fluid. Characterization of the experiments indicates low random error due to manufacturing tolerances. A bias error was found in the Pipe Flow Head Loss experiment. This bias error is believed to be most likely due to an upstream bend in the flow path.

The fabrication approach described here appears to enable the development of experiments that are robust and inexpensive enough to distribute individual copies to small groups of students with the cost to each student in the class comparable to the price of a textbook. This approach opens up the possibility of a wide variety of experimental activities for active learning that can be implemented in classrooms, for home use, and for distance education. Future work will involve bringing students and faculty using the experiments into the design and fabrication loop to enable user-driven modification of the hardware.

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Bibliography


